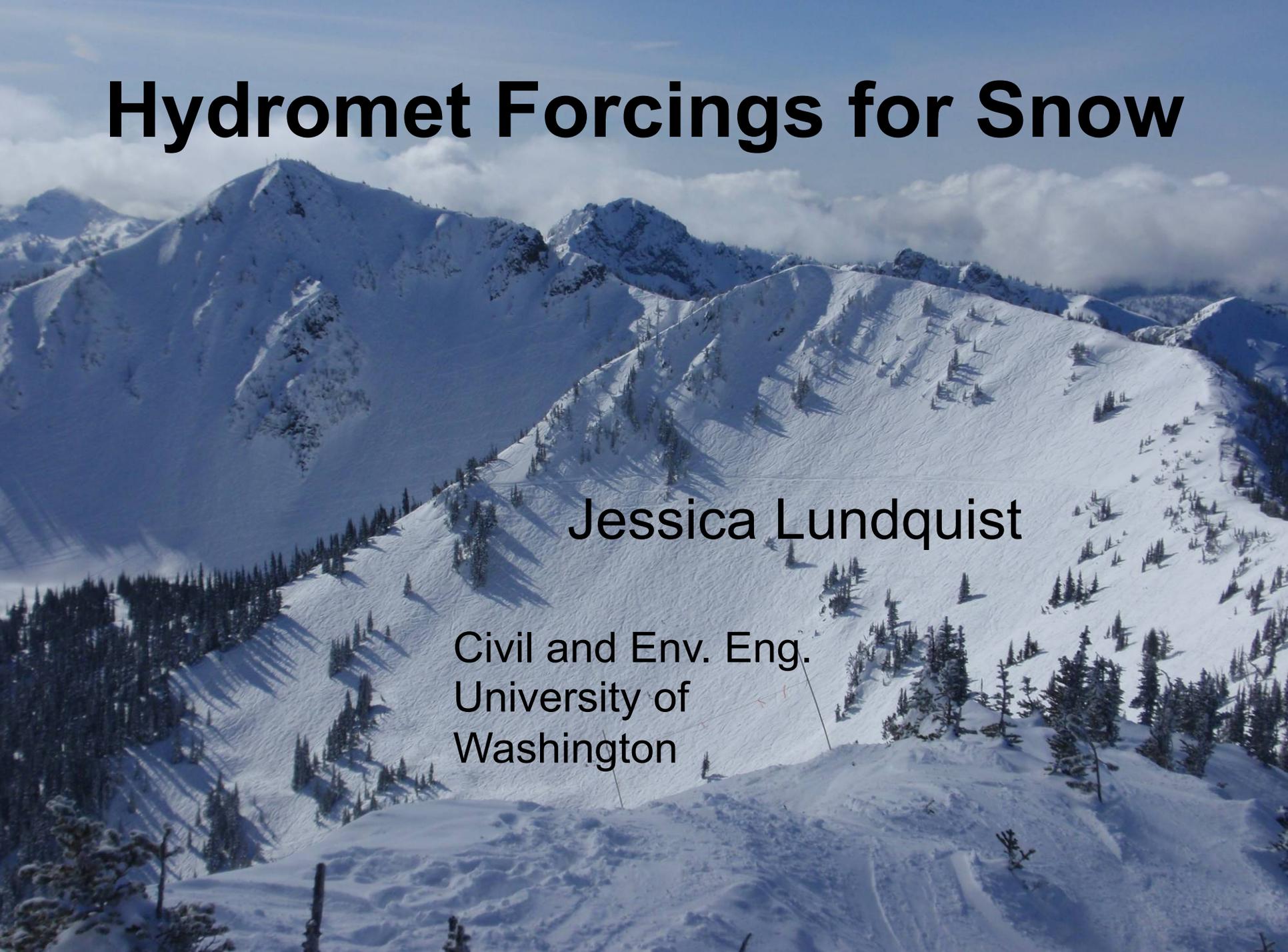


# Hydromet Forcings for Snow



Jessica Lundquist

Civil and Env. Eng.  
University of  
Washington

# Snow



- Major source of water storage and supply in the west (50-80% of annual runoff)
- Most threatened by climate change
- Three part problem:
  - 1) QPE
  - 2) Rain vs. Snow
  - 3) Melt

# Snow



- Major source of water storage and supply in the west (50-80% of annual runoff)
- Most threatened by climate change
- Three part problem:
  - 1) QPE
  - 2) Rain vs. Snow
  - 3) Melt

# Energy for Melt:

- Two approaches
  - Temperature-Index

$$Melt = M_f \cdot (T_i - MBASE)$$

- Full Energy Balance

$$Melt = (1 - \alpha)Q_S + Q_L - \varepsilon\sigma T_S^4 + Q_E + Q_H + Q_R + Q_G - \frac{dU}{dt}$$

# Temperature-Index Model

Example: Snow-17, Anderson 1976

$$Melt = M_f \cdot (T_i - MBASE)$$

Based on air-temperature above a threshold, 0°C

Seasonally-varying melt factor accounts for radiation

- Used operationally
- Hard to beat (Franz et al. 2008)
- Parameters must be calibrated – hard to transfer between sites (He et al. 2011)

# Full Energy Balance Model

Radiation Terms = about 80% of the energy for melt (Marks and Dozier 1992)

$$Melt = (1 - \alpha)Q_S + Q_L - \epsilon\sigma T_S^4 +$$

$$Q_E + Q_H + Q_R + Q_G - \frac{dU}{dt}$$

Turbulent Flux Terms = about 20% of the energy for melt (Marks and Dozier 1992)

Heat from rain and the ground (negligible)

Internal energy of snowpack (heat required to raise to isothermal 0°C)

# For 5-yr horizon, focus on the big one: Radiation

Shortwave Radiation: Incoming - Reflected

$$Melt = (1 - \alpha)Q_S + Q_L - \epsilon\sigma T_S^4$$

albedo

Incoming Longwave

Outgoing Longwave: depends on snow surface temperature

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albedo

Incoming Longwave

Outgoing Longwave: depends on snow surface temperature

None of these are measured at a typical snow site.

# Conditions good for snow are bad for observations.

- Harsh weather
  - Power limitations
  - Difficult access
  - Infrequent maintenance
- = Temporal and Spatial gaps  
(missing data must be estimated)

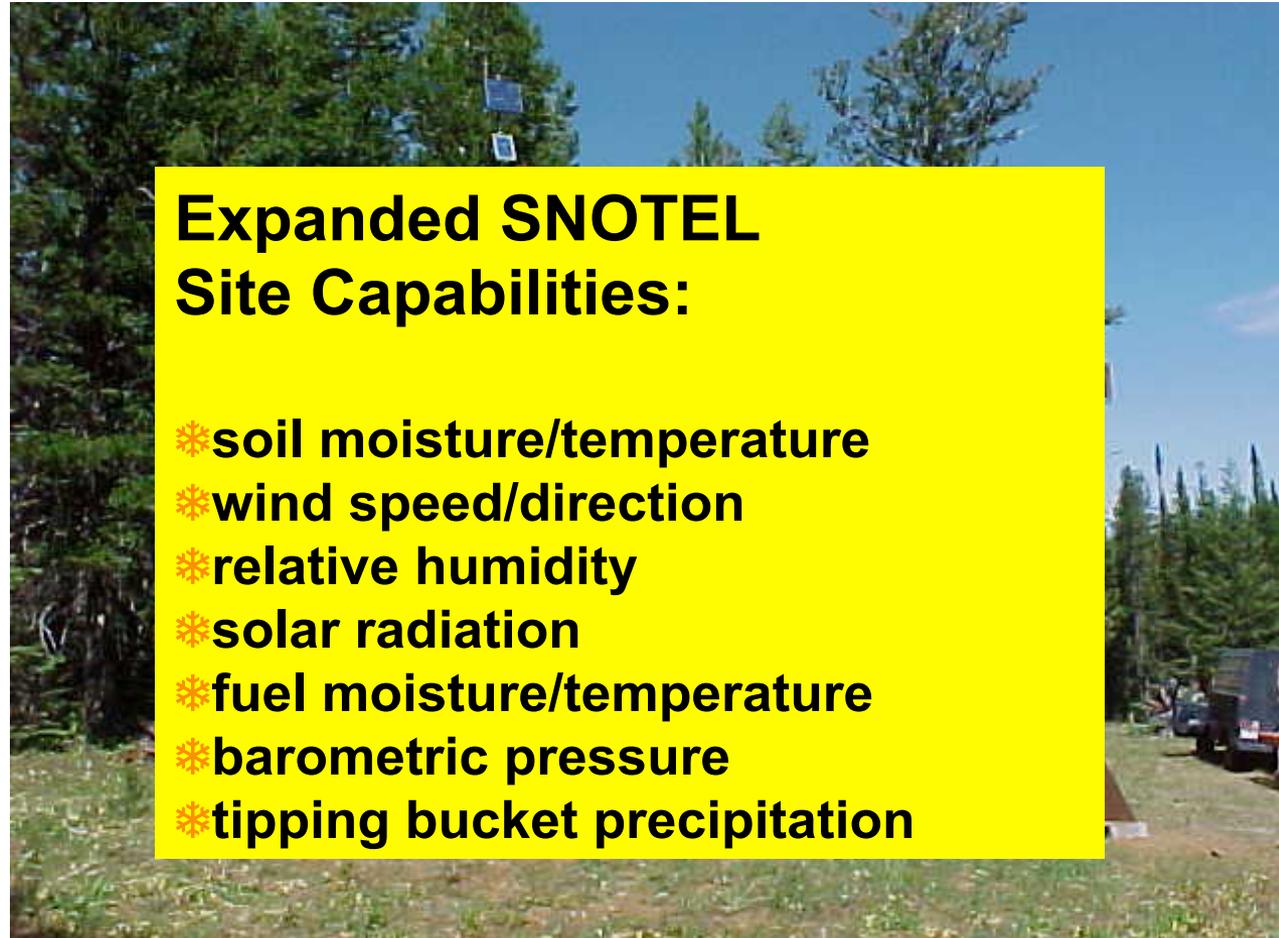


Onion Creek HMT station April 2011  
(photo courtesy of Nic Wayand)

# SNOTEL LAYOUT

## Standard SNOTEL Site Components:

- \*snow pillow
- \*snow depth sensor
- \*precipitation gauge
- \*temperature sensor



## Expanded SNOTEL Site Capabilities:

- \*soil moisture/temperature
- \*wind speed/direction
- \*relative humidity
- \*solar radiation
- \*fuel moisture/temperature
- \*barometric pressure
- \*tipping bucket precipitation

# Even at enhanced snotel, only incoming shortwave is measured

Shortwave Radiation: Incoming - Reflected

$$Melt = (1 - \alpha) Q_S + Q_L - \epsilon \sigma T_S^4$$

albedo

Incoming Longwave

Outgoing Longwave: depends on snow surface temperature

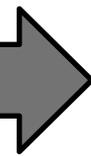
## Limited Variables Measured

Temp    Precip    Relative Humidity    Wind    NetRad    SWin    LWin



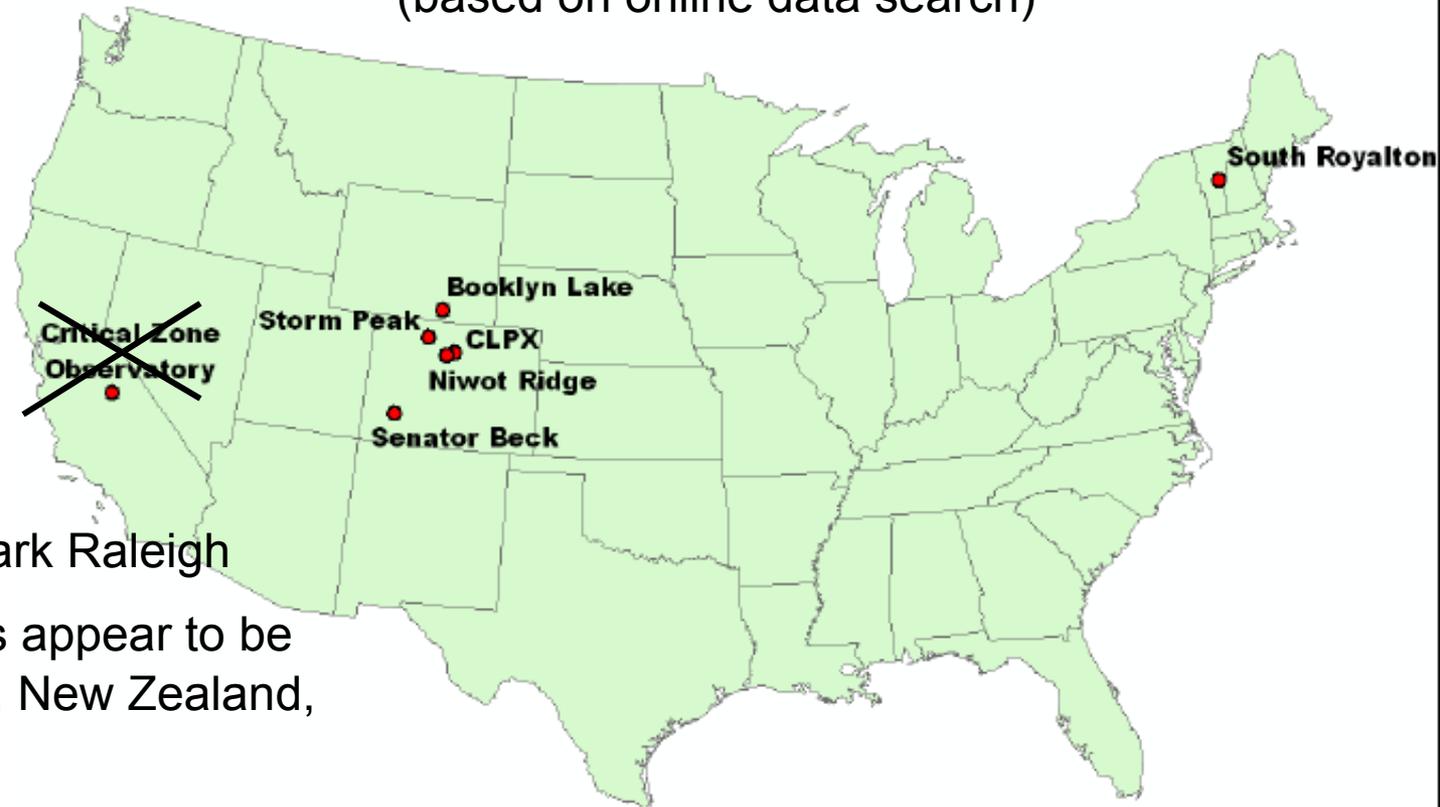
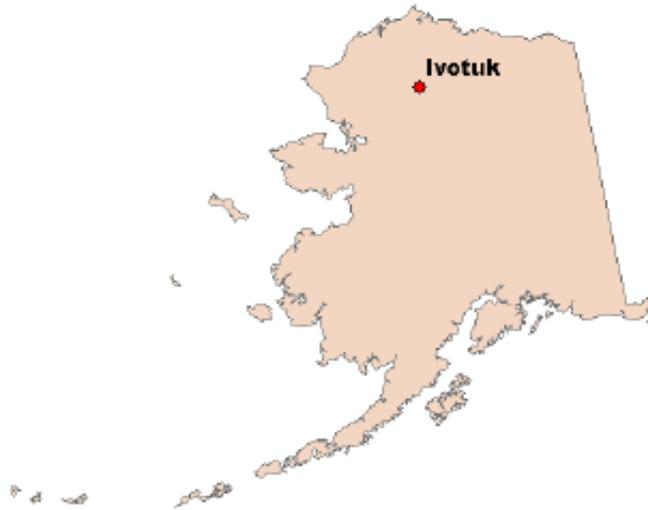
Common

Rare



# Sites with co-located snow and LW radiation measurements of any duration

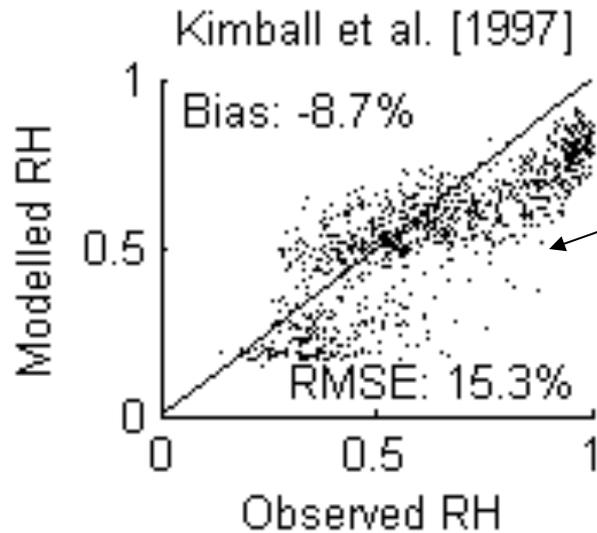
(based on online data search)



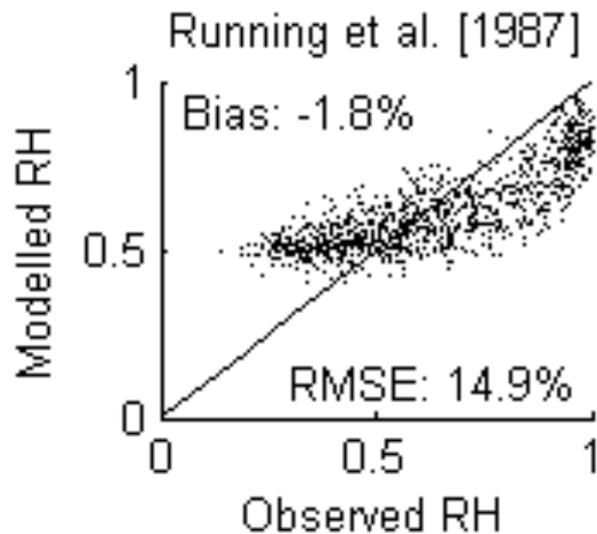
Slide courtesy of Mark Raleigh

Note: good datasets appear to be available in Norway, New Zealand, and Switzerland

# Estimation methods often not transferable from continental to maritime mountains: Testing Relative Humidity in California HMT

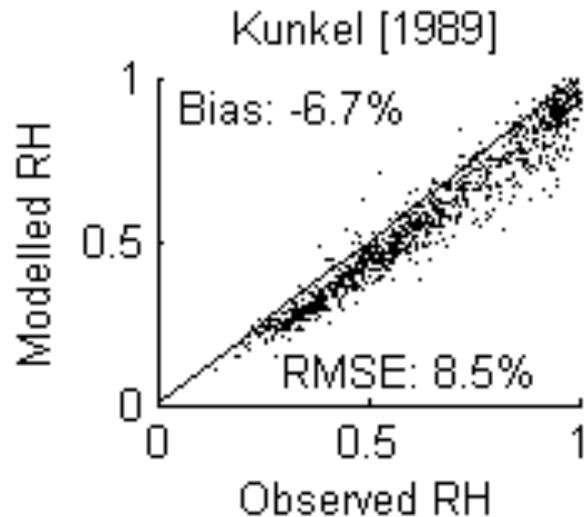


Estimating RH at a point, based on Tmin

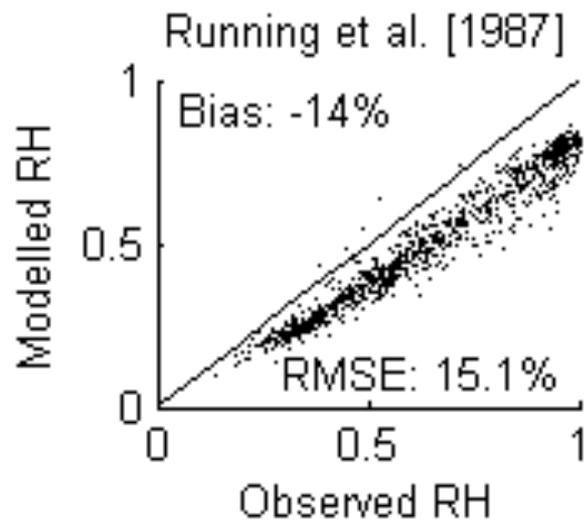


Graphic courtesy of Shara Feld

# Estimation methods often not transferable from continental to maritime mountains: Testing Relative Humidity in California HMT

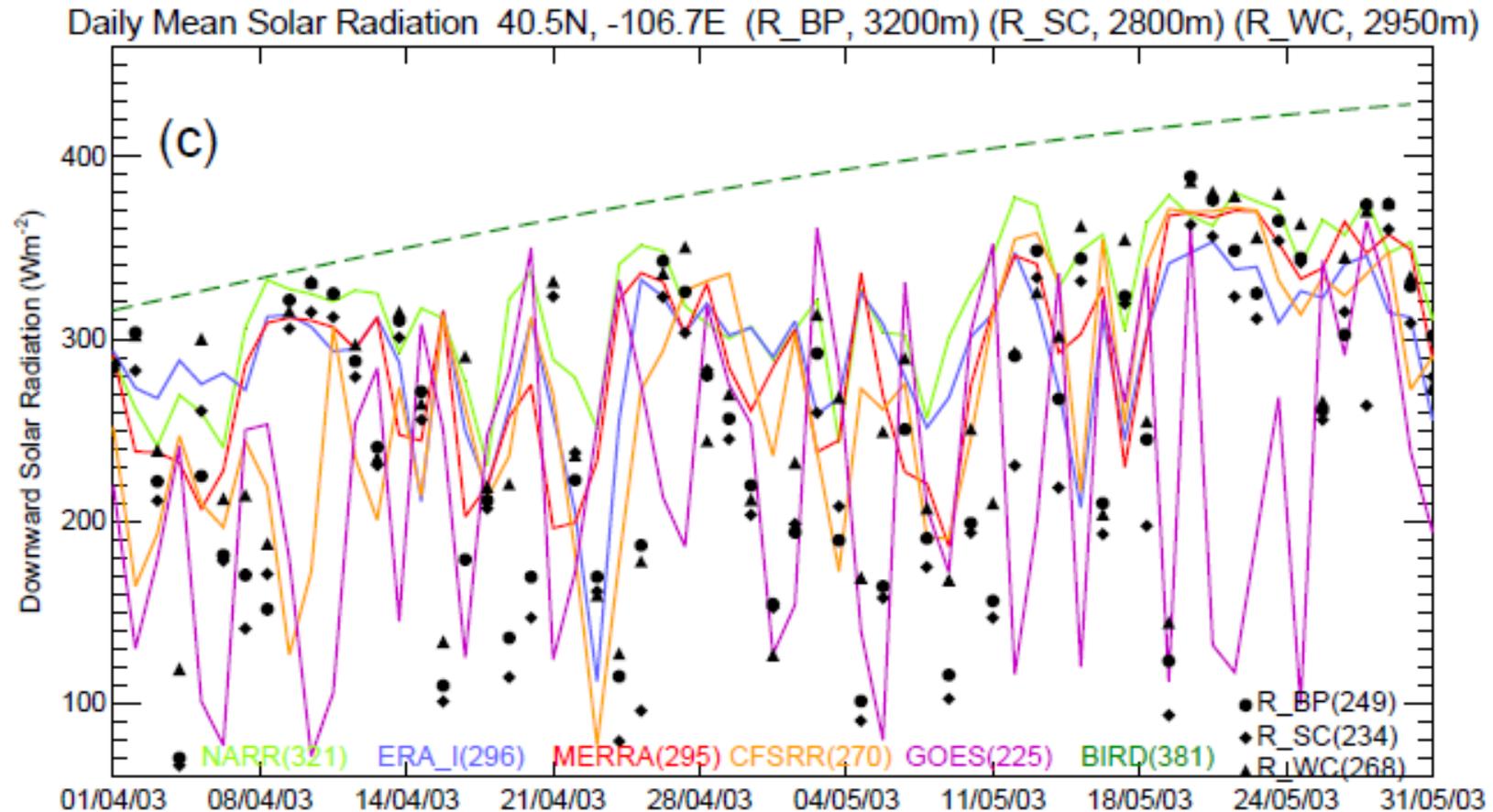


← Estimating RH at another location, given one RH measurement in the basin



Graphic courtesy of Shara Feld

# Satellite and Reanalysis Products: Promising but need more validation

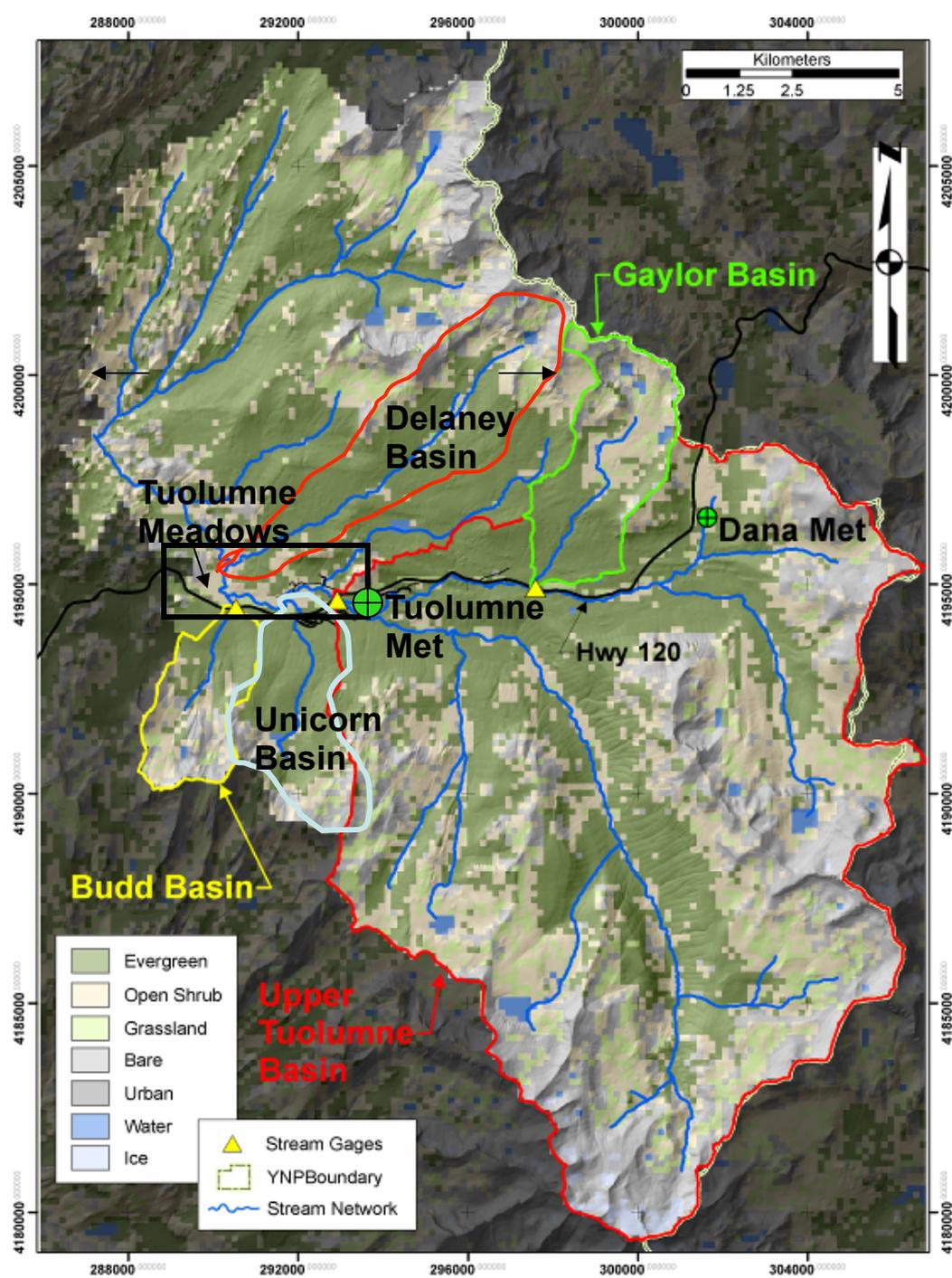


Graphic courtesy of Drew Slater, showing various Reanalysis and Satellite products vs. surface measurements at Rabbit Ears during CLP-X

# So do these issues really matter for streamflow?



- We have the computing power for physically-based, distributed models
- But do we have the observations to support them?



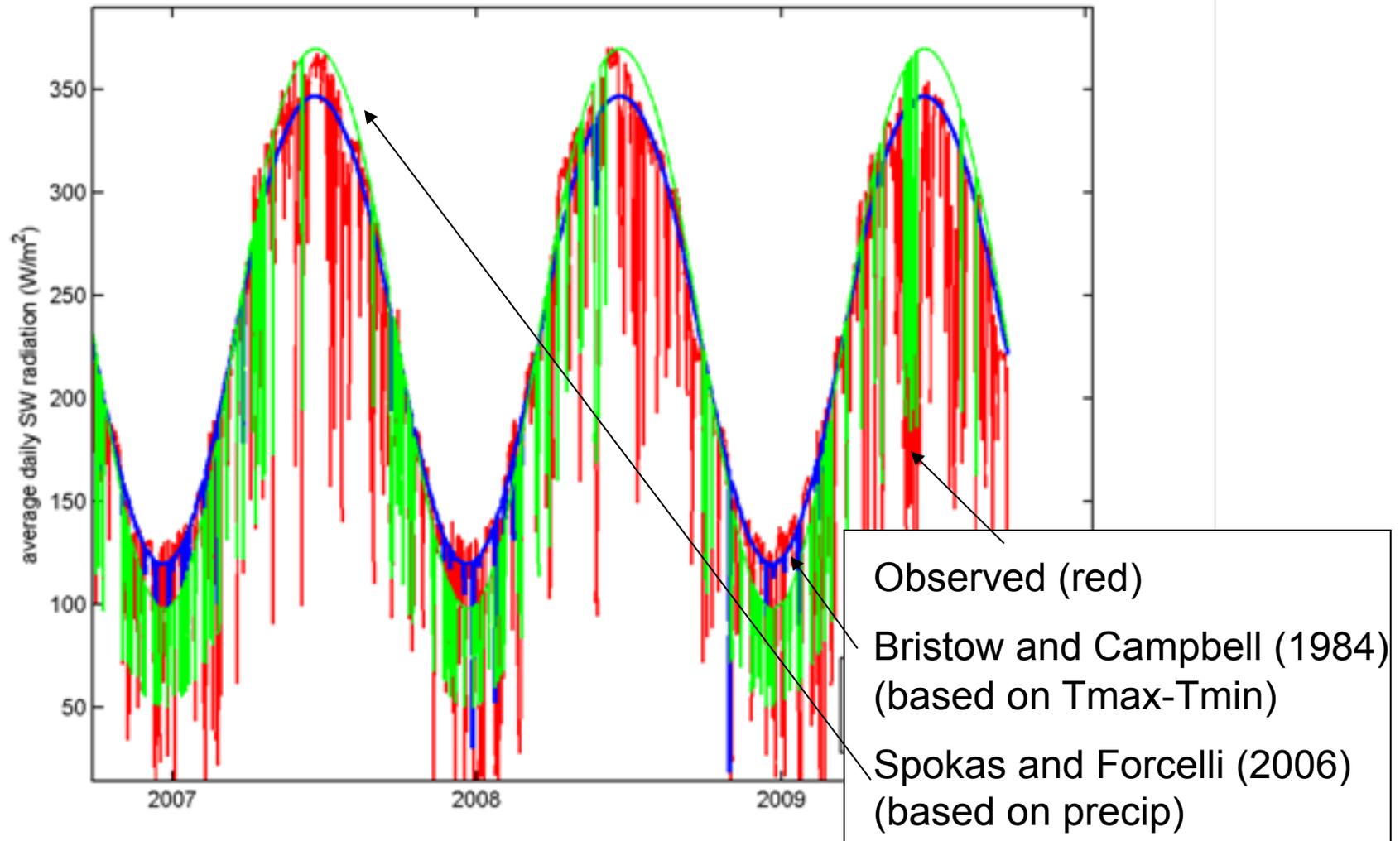
## Example:

Modeling Tuolumne River in Yosemite, California with the Distributed Hydrology Soil Vegetation Model (DHSVM)

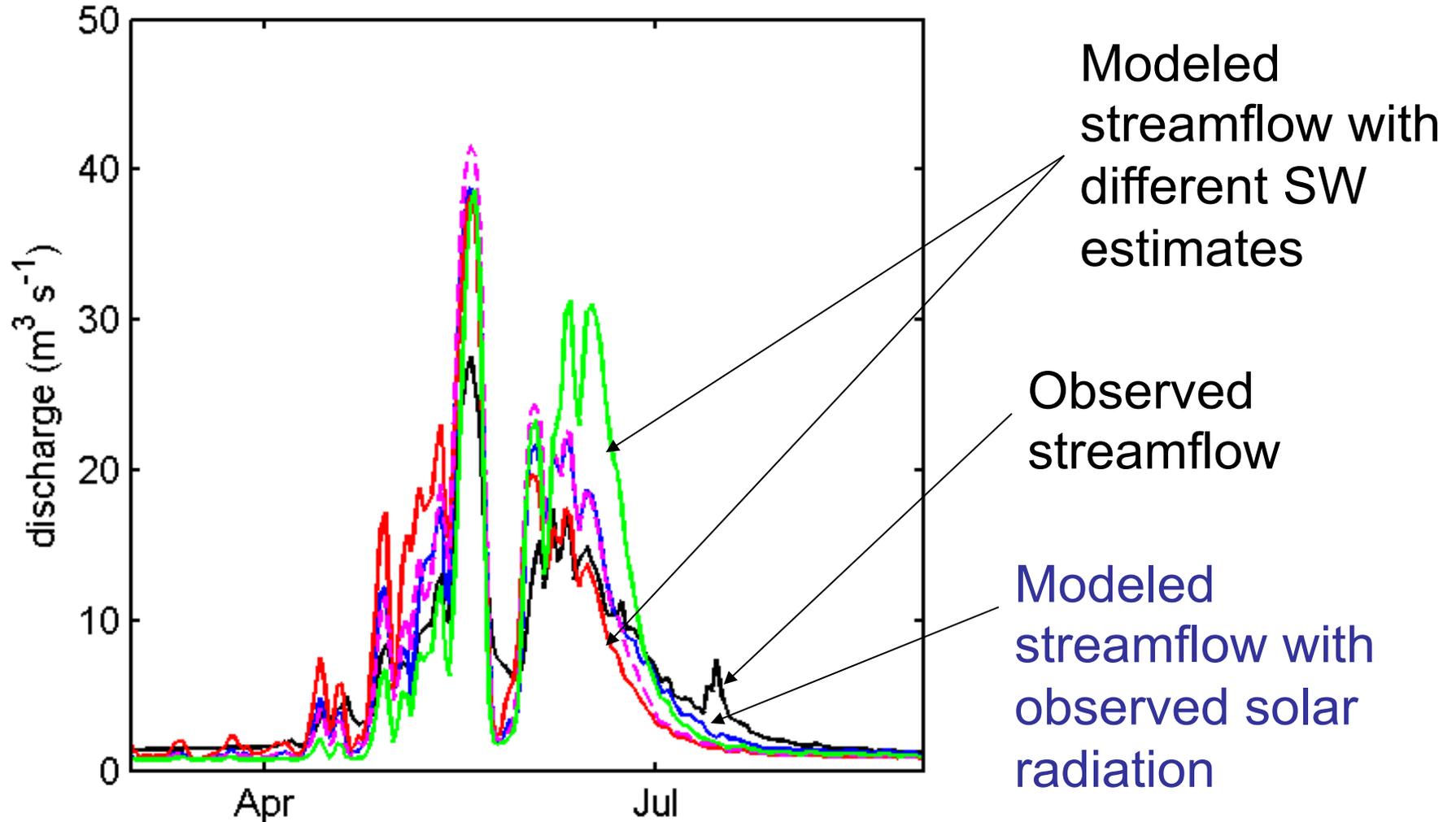
-High altitude, sunny Sierra, granite-lined

-Essentially all snow, little to no baseflow

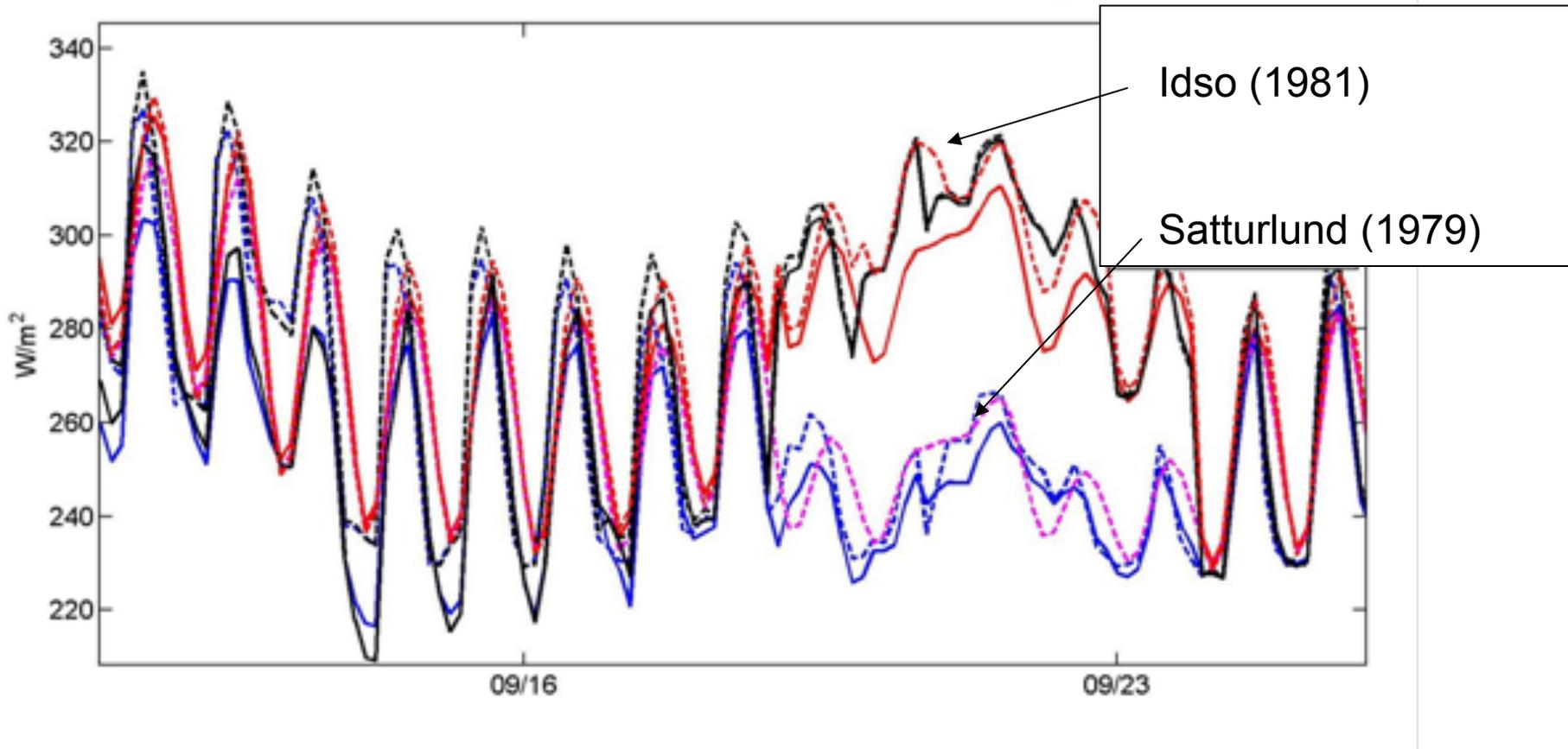
# Daily average SW radiation: observed and 2 different estimates



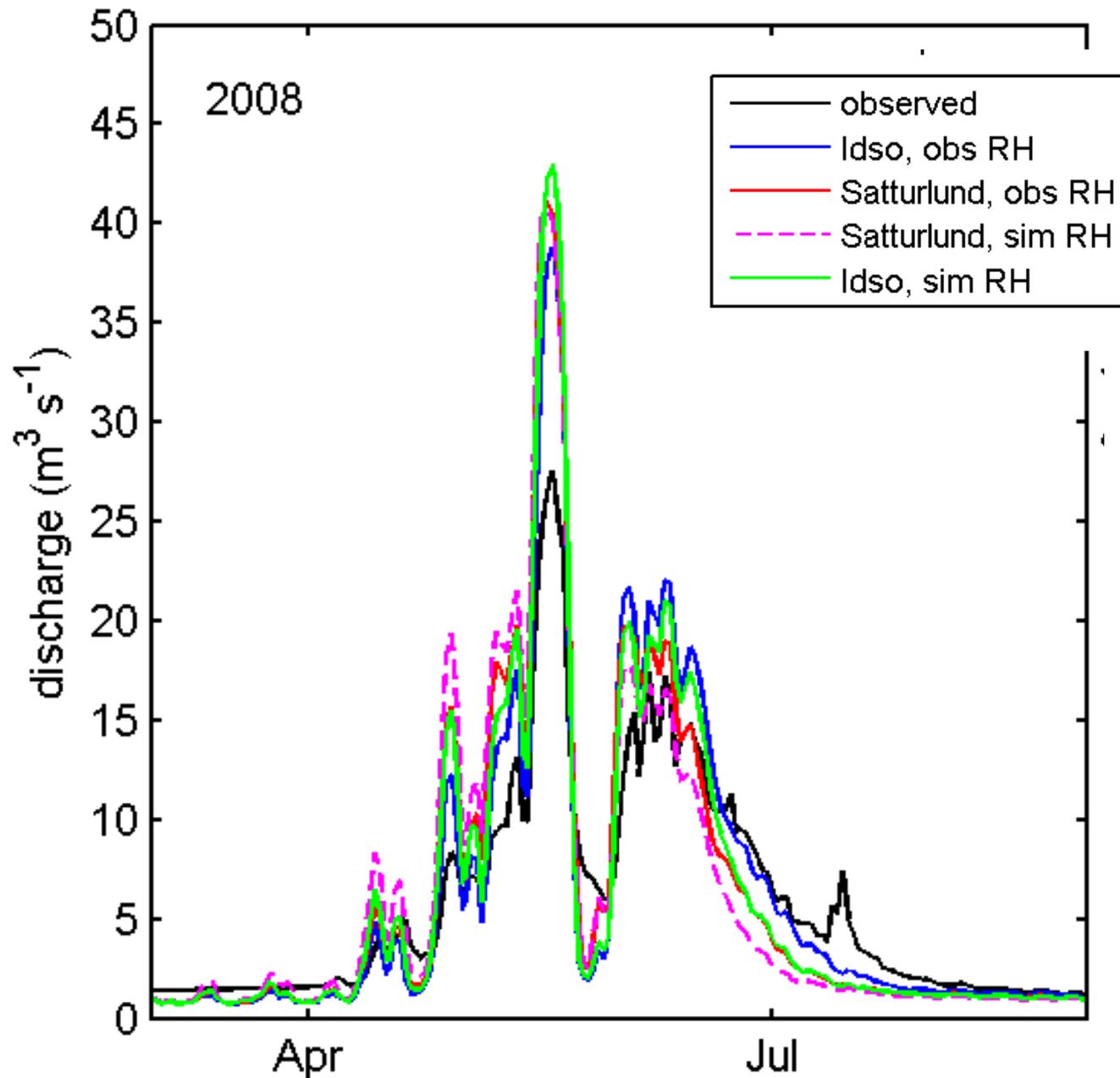
Modeled snowfed streamflow (particularly late season) is sensitive to how you parameterize solar radiation.



# Incoming LW radiation not measured, estimated from humidity and diurnal T range



Solid lines are with observed RH; Dashed lines with estimated RH



Streamflow is sensitive to the LW algorithm chosen and to whether relative humidity is estimated or measured

# Concluding Thoughts

- Most areas (especially higher elevations) dominated by radiation (SW + LW) – we need to measure and/or estimate this better
- Instruments will only be useful if properly maintained – not trivial
- We can equip Snotel with upward and downward pyranometers (SW & albedo) + infrared snow temperature (outgoing LW)
- Incoming longwave will require representative snow observatories with dedicated staffing (could only afford a few, so need remote sensing and/or estimation techniques that work)

FLERCHINGER ET AL.: ATMOSPHERIC LONG-WAVE RADIATION ALGORITHMS

**Table 1.** Algorithms for Estimating Clear-Sky Emissivity Following the Form of the Stefan-Boltzmann Equation or for Estimating Downwelling Long-wave Radiation Directly<sup>a</sup>

Source	Clear-Sky Algorithm
Ångström [1918] <sup>b</sup>	$\epsilon_{cb} = (0.83 - 0.18 \times 10^{-0.067e_o})$
Brunt [1932] <sup>b</sup>	$\epsilon_{cb} = (0.52 + 0.205\sqrt{e_o})$
Brutsaert [1975]	$\epsilon_{cb} = 1.723 \left(\frac{e_o}{T_o}\right)^{1/7}$
Garratt [1992]	$\epsilon_{cb} = 0.79 - 0.17 \exp(-0.96e_o)$
Idso and Jackson [1969]; referred to as Idso-1	$\epsilon_{cb} = 1 - 0.261 \exp(-0.00077(T_o - 273.16)^2)$
Idso [1981]; referred to as Idso-2	$\epsilon_{cb} = 0.7 + 5.95 \times 10^{-4} e_o \exp\left(\frac{1500}{T_o}\right)$
Iziomon et al. [2003] <sup>d</sup>	$\epsilon_{cb} = 1 - X \exp\left(\frac{-Ye_o}{T_o}\right)$
Keding [1989]	$\epsilon_{cb} = 0.92 - 0.7 \times 10^{-1.2e_o}$
Niemelä et al. [2001]	$\epsilon_{cb} = \begin{cases} 0.72 + 0.09(e_o - 0.2) & \text{for } e_o \geq 0.2 \\ 0.72 - 0.76(e_o - 0.2) & \text{for } e_o < 0.2 \end{cases}$
Prata [1996] <sup>c</sup>	$\epsilon_{cb} = 1 - (1 + w) \exp(-(1.2 + 3w)^{1/2})$
Satterlund [1979]	$\epsilon_{cb} = 1.08[1 - \exp(-(10e_o)^{T_o}/2016)]$
Swinbank [1963]	$L_{clr} = 5.31 \times 10^{-13} T_o^6$
Dilley and O'Brien [1998] <sup>c</sup>	$L_{clr} = 59.38 + 113.7 \left(\frac{T_o}{273.16}\right)^6 + 96.96\sqrt{w/25}$

Used in several Land Surface Models

Used in Liston snowmodel

Used in Vic, dhsvm and UEB

recommended

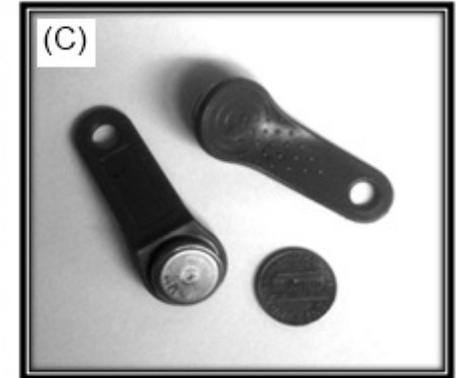
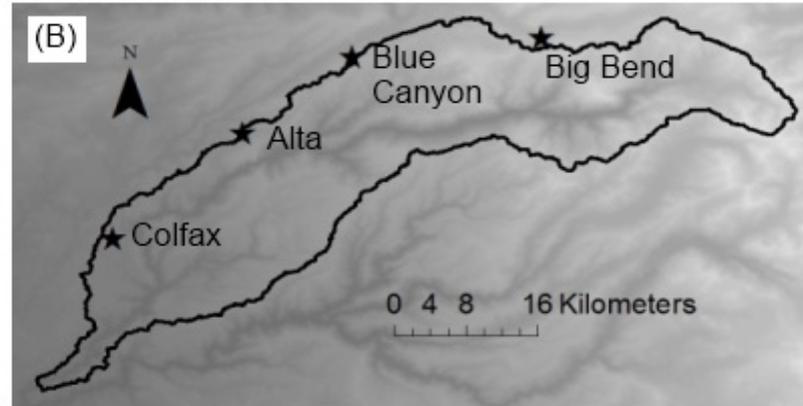
<sup>a</sup>Coefficients are based on vapor pressure ( $e_o$ ) in kilopascals, temperature ( $T_o$ ) in kelvins, and precipitable water ( $w$ ) in centimeters.

<sup>b</sup>As cited by Niemelä et al. [2001].

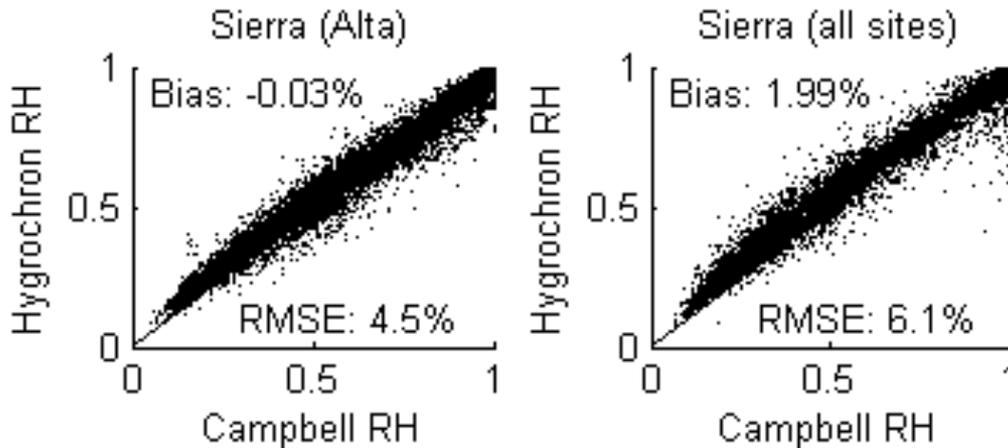
<sup>c</sup> $w = 4650e_o/T_o$  [Prata, 1996].

<sup>d</sup>Values for  $X$  and  $Y$  in the algorithm of Iziomon et al. [2003] were interpolated between a lowland site at 212-m elevation ( $X = 0.35$  and  $Y = 100 \text{ K kPa}^{-1}$ ) and a mountain site at 1489-m elevation ( $X = 0.43$  and  $Y = 115 \text{ K kPa}^{-1}$ ).

# But RH sensors are cheap and easy



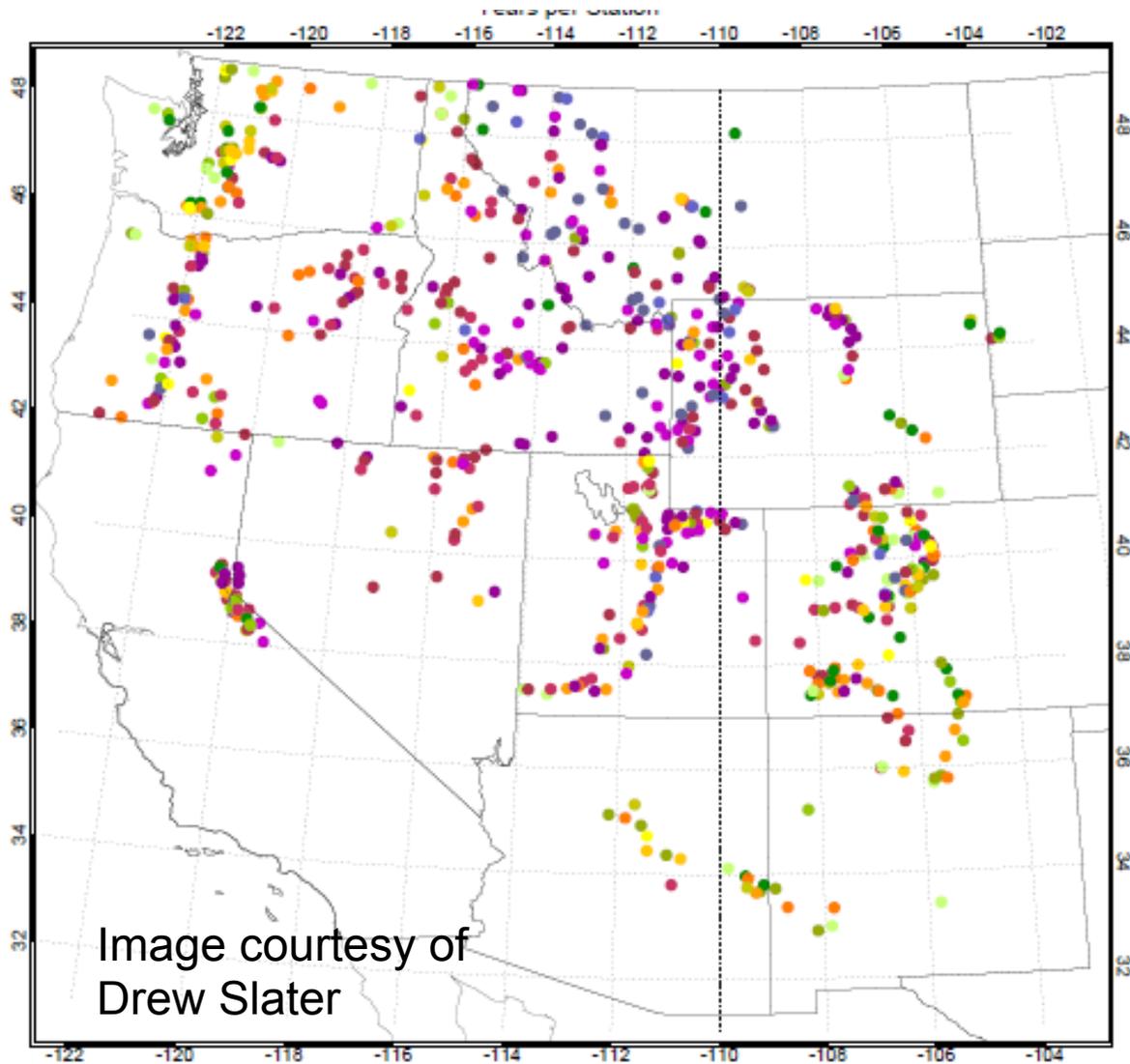
(C) iButton measurements in the Sierra Nevada



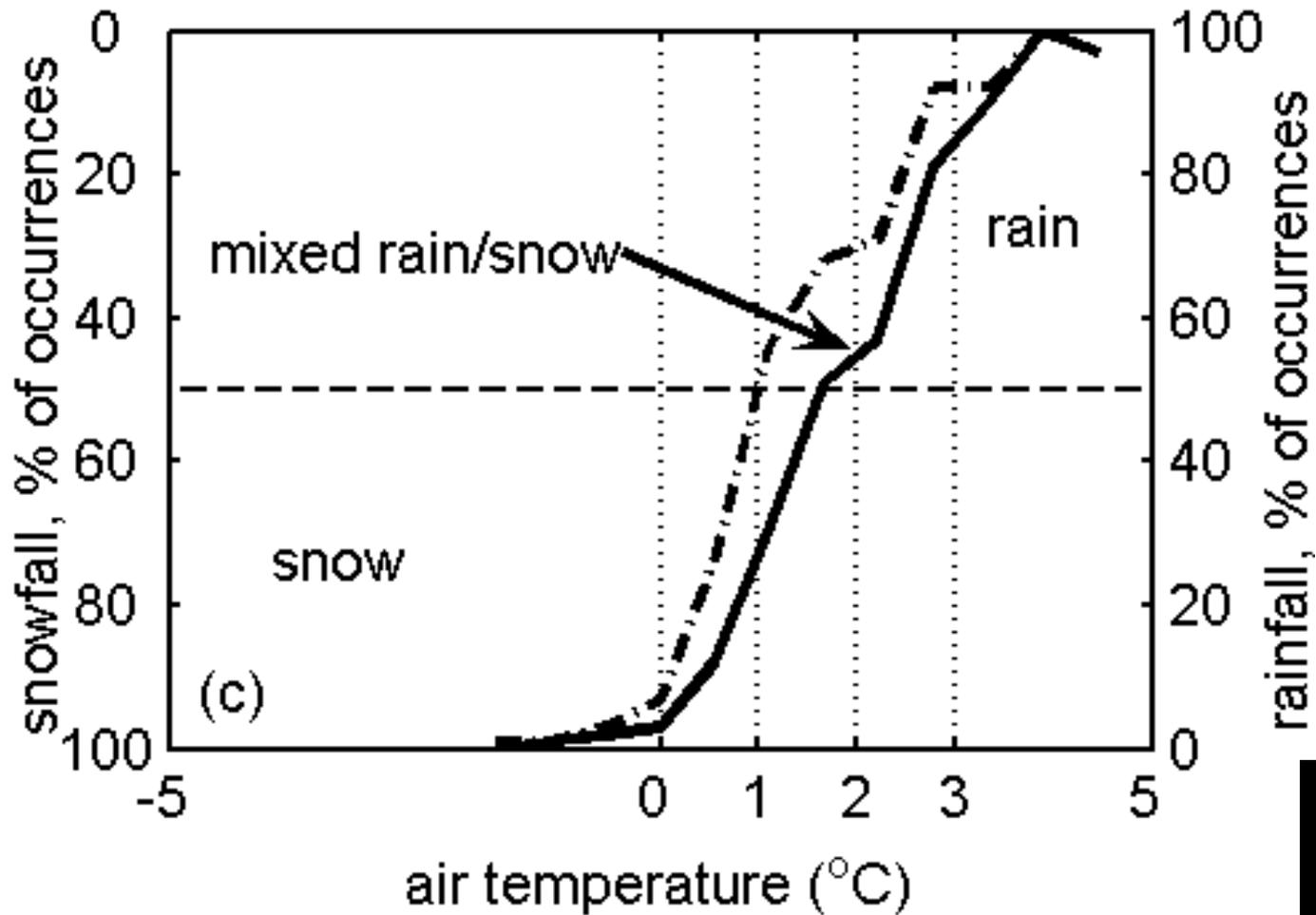
Graphic courtesy of Shara Feld, from Feld and Lundquist, submitted to WRR

**Extra Slides Follow**

# Map of Snotel Sites



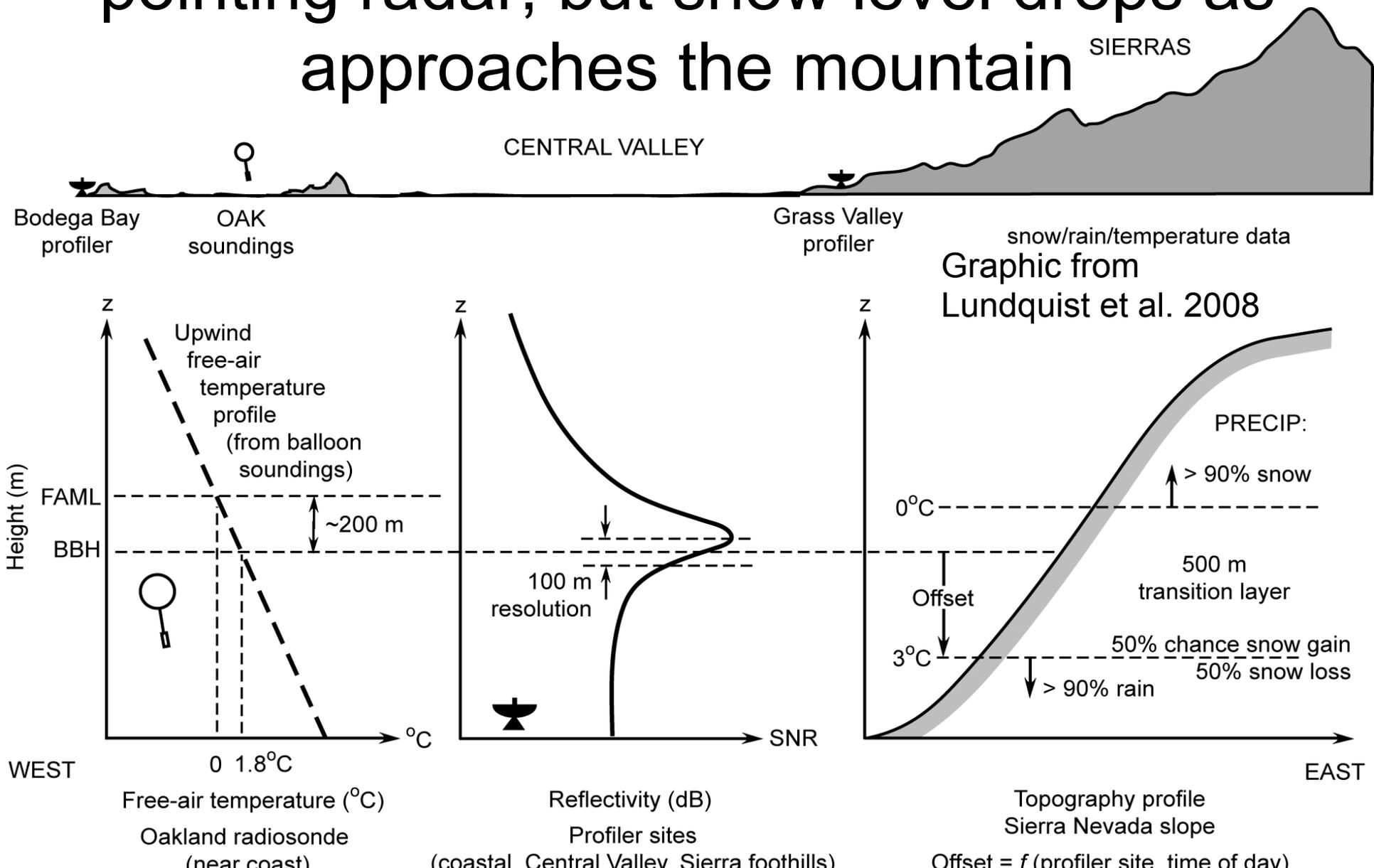
# First, determine whether rain, snow, or a wintry mix



Graphic from US Army Corps of Engineers in *Snow Hydrology*, 1956



# Can get rain vs snow from vertically-pointing radar, but snow level drops as approaches the mountain



# Where does snow change to rain?

## Surface Validation Options:

- Human observers
- Laser disdrometer
- Co-located precip and snow depth + snow pillow to determine fate of precip on the surface
- Digital camera (web cam)



Path Forward: Partner with  
Transportation Agencies



# Full Energy Balance Model

- Physically based, but when we estimate all the input, it has many more tunable parameters than the temperature index model

$$Melt = (1 - \alpha)Q_S + Q_L - \epsilon\sigma T_S^4 + Q_E + Q_H + Q_R + Q_G - \frac{dU}{dt}$$

# How do we arrive at solar radiation in snow modeling?

- 1) **Use latitude, longitude, solar geometry to calculate potential radiation**
- 2) **Modify potential radiation for slope, aspect, shading by surrounding topography**
- 3) Determine some transmittance factor (or other scaling) to decrease potential radiation based on clouds/atmospheric moisture content
- 4) Further reduce solar radiation for areas under forest cover

These are pretty good.

# How do we arrive at solar radiation in snow modeling?

- 1) Use latitude, longitude, solar geometry to calculate potential radiation
- 2) Modify potential radiation for slope, aspect, shading by surrounding topography
- 3) Determine some transmittance factor (or other scaling) to decrease potential radiation based on clouds/atmospheric moisture content**
- 4) Further reduce solar radiation for areas under forest cover

This is generally a big guess.

Based on T<sub>max</sub>-T<sub>min</sub> and/or Precip

# Commonly used formulas

Bristow and Cambell, 1984

$$R_s = R_a[A[1 - \exp(-B(\Delta T)^C)]]$$

Hargreaves and Samami, 1985

$$R_s = R_a(k_R)\sqrt{(T_{\max} - T_{\min})}$$

$R_a$  is potential radiation (from geometry)

A, B, C, and  $k_R$  are empirical coefficients.

Both are based on the diurnal temperature range.

# Alternate method is to look at precipitation records to determine transmissivity

TABLE 1. Decision matrix used to assign value for atmospheric transmissivity ( $\tau$ ).

Conditions	Value of $\tau$
No precipitation at $\Delta T > 10\text{C}$ (assumed clear sky conditions)	$\tau = 0.70$
No precipitation today, but precipitation fell the previous day	$\tau = 0.60$
Precipitation occurring on present day	$\tau = 0.40$
Precipitation today and also the previous day	$\tau = 0.30$

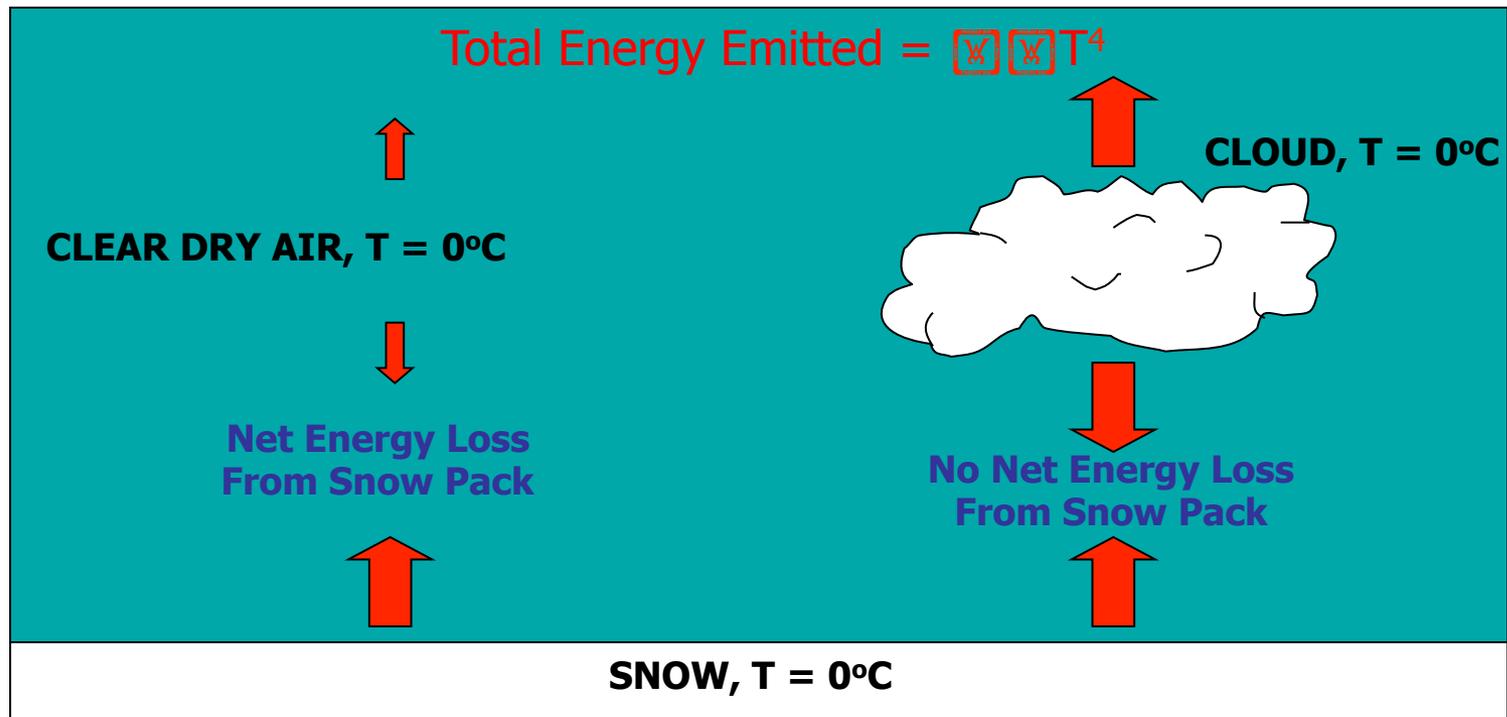
<sup>a</sup>  $\Delta T$  is defined as ( $T_{\text{air}_{\text{max}}} - T_{\text{air}_{\text{min}}}$ ).

# How do we arrive at longwave radiation in snow modeling?

- 1) Estimate the emissivity of the atmosphere. (Function of  $T_{\max}$ - $T_{\min}$  and Relative Humidity)
- 2) Estimate the effective temperature of the atmosphere. (May adjust for clouds)
- 3) Use the Stefan-Boltzmann equation.
- 4) Can also add in longwave emitted from surrounding terrain
- 5) Further modify longwave for areas under forest cover

# Snow Energy Exchanges

- Atmospheric (Longwave) Radiation

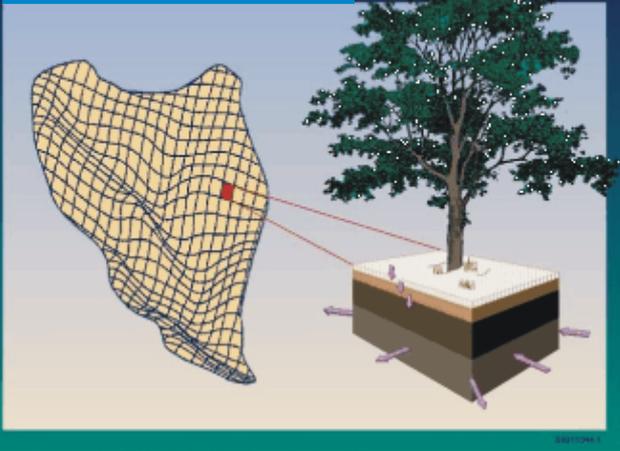


<u>Emissivity</u>	
Air	0.60 - 0.70
Water, Ice, Snow	0.92 - 0.97

Slide from  
Danny Marks



## Model Diagram



# DHSVM

- Distributed model at 150m resolution. (39,348 grid cells in North Fork Basin)
- Simulates vertical and horizontal fluxes of water through vegetation, snow and soil.
- Used extensively for Land use change and Climate change research. (Wigmosta et al. 1994)

Topographic Shading

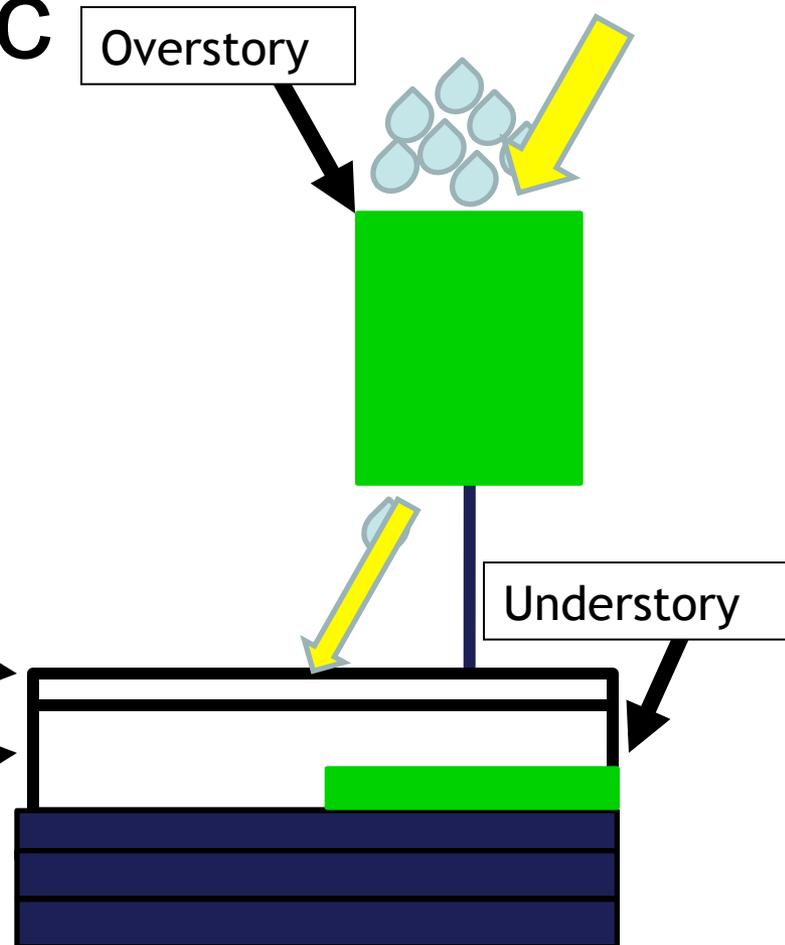
Vegetation Map

Soil Depth Map

Elevation

# DHSVM Snow Model Schematic

- Two Layer Vegetation
  - Precipitation Interception and Fall through
  - Radiation attenuation
  - Aerodynamic attenuation
- Two Layer Snow pack
  - Surface → Controls fluxes
  - Pack → Stores Energy, Water, Ice etc.



# Energy Balance

- $Q_{net} = (Q_r + Q_s + Q_e + Q_p) * dt$
- $Q_r = \text{NetRad}$
- $Q_s = \text{Sensible Heat}$
- $Q_e = \text{Latent Heat}$
- $Q_p = \text{Advected energy via the input of water}$
  
- $Q_{net} > 0 \rightarrow$  Warms pack to 0°C, then melts
- $Q_{net} < 0 \rightarrow$  Refreezes water, then cools

# Energy Balance approach requires more Meteorological Input

What is required at each time step:

Temperature

Precipitation

Wind Speed

Relative Humidity

Shortwave Rad

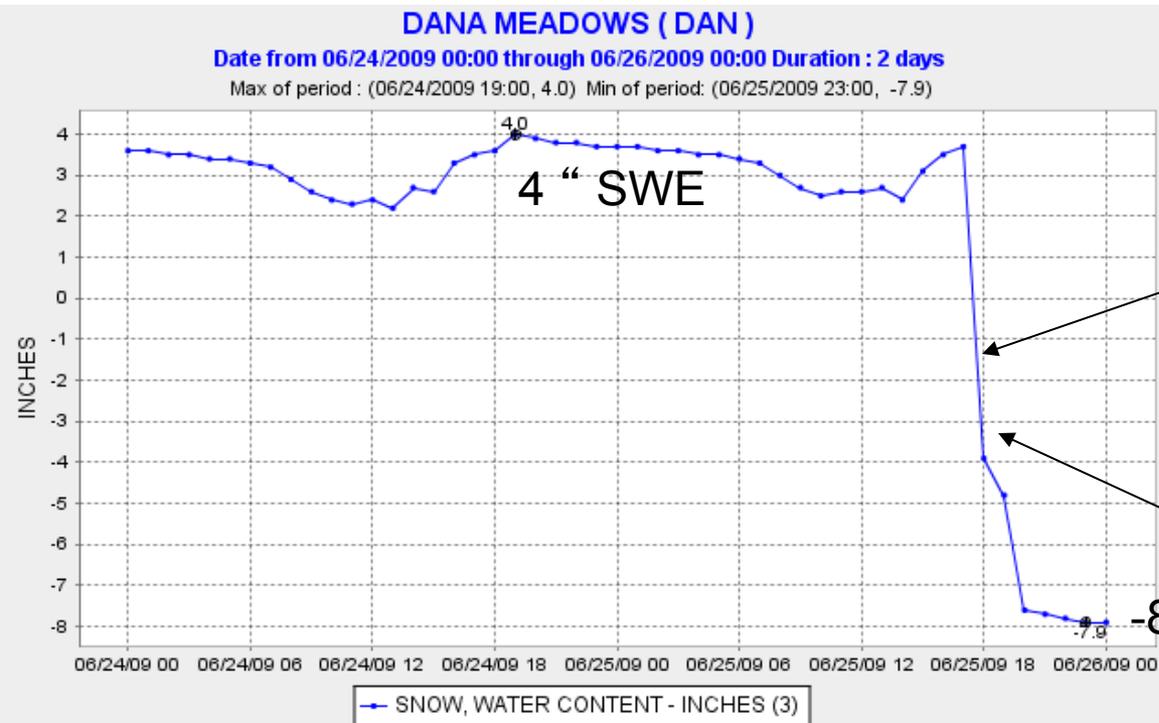
Longwave Rad

# Let's visit the Dana Meadows snow pillow.

June 25, 2009



# Dana snow pillow, evening of June 25 2009



12" SWE difference before and after this event.

# How long does it take a tree to grow?

